

# 4-4 Prove Triangles Congruent by SAS and HL

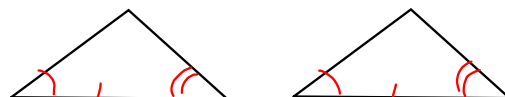
## 4-5 ASA and AAS

SSS  
SAS  
ASA  
AAS  
HL

Theorem 4.5 HL (Hypotenuse-Leg)-If the hypotenuse and a leg of one right  $\triangle$  are  $\cong$  to the hypotenuse and one leg of another right  $\triangle$ , then the  $\triangle$ s are  $\cong$ .



Postulate 21 ASA-If 2 angles and the included side of one  $\triangle$  are  $\cong$  to 2 angles and the included side of another triangle, then the triangles are  $\cong$ .



Given:  $\overline{AB} \parallel \overline{ED}$ ;  $\overline{AB} \cong \overline{ED}$   
Prove:  $\triangle ABC \cong \triangle DEC$

S.

①  $\overline{AB} \parallel \overline{ED}$   
 $\overline{AB} \cong \overline{ED}$

②  $\angle E \cong \angle B$   
 $\angle D \cong \angle A$

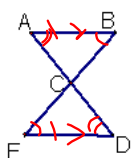
③  $\triangle ABC \cong \triangle DEC$

R.

① Given

② Alt Int  $\angle$ s thm

③ ASA

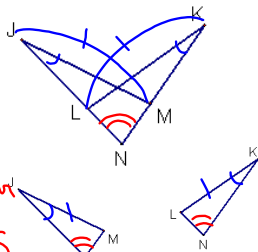


Theorem 4.6 AAS-If 2 angles and a non-included side of one  $\triangle$  are  $\cong$  to 2 angles and a non-included side of another  $\triangle$ , then the  $\triangle$ s are  $\cong$ .



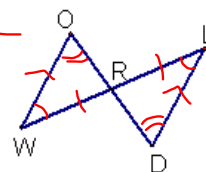
Given:  $\angle K \cong \angle J$ ,  $\overline{KL} \cong \overline{JM}$   
 Prove:  $\overline{LN} \cong \overline{MN}$

- |                                       |             |
|---------------------------------------|-------------|
| ① ~                                   | ① Given     |
| ② $\angle N \cong \angle N$           | ② Reflexive |
| ③ $\triangle JNM \cong \triangle KNL$ | ③ AAS       |
| ④ $\overline{LN} \cong \overline{MN}$ | ④ CPCTC     |



Given:  $\overline{WO} \parallel \overline{LD}$ , R is the midpoint of  $\overline{WL}$   
 Prove:  $\overline{OR} \cong \overline{DR}$

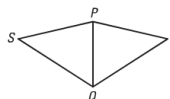
- |  |                         |
|--|-------------------------|
| ① ~  | ① Given                 |
| ② $\overline{WR} \cong \overline{RL}$                    | ② def of midpoint       |
| ③ $\angle W \cong \angle L$<br>$\angle O \cong \angle D$ | ③ Alt int $\angle$ s th |
| ④ $\triangle WOR \cong \triangle LDR$                    | ④ AAS                   |
| ⑤ $\overline{OR} \cong \overline{DR}$                    | ⑤ CPCTC                 |



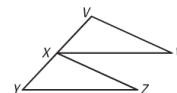
HW  
 p245-246 #s 35-37  
 p252-255 #s 3-5, 7, 33, 34

**PROOF** In Exercises 35 and 36, write a proof.

35. **GIVEN**  $\triangleright \overline{PQ}$  bisects  $\angle SPT$ ,  $\overline{SP} \cong \overline{TP}$   
**PROVE**  $\triangleright \triangle SPQ \cong \triangle TPQ$

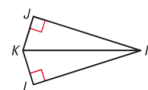


36. **GIVEN**  $\triangleright \overline{VX} \cong \overline{XW}$ ,  $\overline{XW} \cong \overline{YZ}$ ,  $\overline{XW} \parallel \overline{YZ}$   
**PROVE**  $\triangleright \triangle VXW \cong \triangle XYZ$



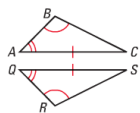
**PROOF** In Exercises 37 and 38, write a proof.

37. **GIVEN**  $\triangleright \overline{JM} \cong \overline{LM}$   
**PROVE**  $\triangleright \triangle JKM \cong \triangle LKM$

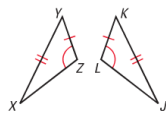


**IDENTIFY CONGRUENT TRIANGLES** Is it possible to prove that the triangles are congruent? If so, state the postulate or theorem you would use.

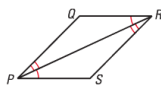
3.  $\triangle ABC, \triangle QRS$



4.  $\triangle XYZ, \triangle JKL$

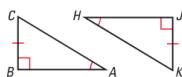


5.  $\triangle PQR, \triangle RSP$



7. **★ MULTIPLE CHOICE** Which postulate or theorem can you use to prove that  $\triangle ABC \cong \triangle HJK$ ?

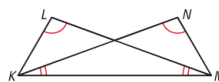
- (A) HL (B) AAS  
(C) SAS (D) Not enough information



33. **PROOF** Write a proof.

**GIVEN**  $\angle NKM \cong \angle LMK, \angle L \cong \angle N$

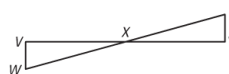
**PROVE**  $\triangle NMK \cong \triangle LKM$



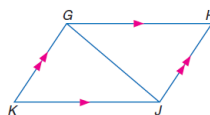
34. **PROOF** Write a proof.

**GIVEN**  $X$  is the midpoint of  $\overline{VY}$  and  $\overline{WZ}$ .

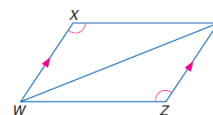
**PROVE**  $\triangle VWX \cong \triangle YZX$



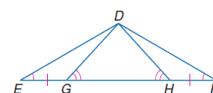
4. Given:  $\overline{GH} \parallel \overline{KJ}, \overline{GK} \parallel \overline{HJ}$   
Prove:  $\triangle GJK \cong \triangle JGH$



5. Given:  $\overline{XW} \parallel \overline{YZ}, \angle X \cong \angle Z$   
Prove:  $\triangle WXY \cong \triangle YZW$

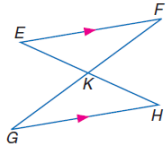


7. Given:  $\angle E \cong \angle K, \angle DGH \cong \angle DHG$   
 $\overline{EG} \cong \overline{KH}$   
Prove:  $\triangle EGD \cong \triangle KHD$



9. Given:  $\overline{EF} \parallel \overline{GH}$ ,  $\overline{EF} \cong \overline{GH}$

Prove:  $\overline{EK} \cong \overline{KH}$



11. Given:  $\angle V \cong \angle S$ ,  $\overline{TV} \cong \overline{QS}$

Prove:  $\overline{VR} \cong \overline{SR}$

